

$$AF + BD + CE = s \left[1 + \frac{(a-b)(b-c)(c-a)}{abc} \right],$$

$$FB + DC + EA = s \left[1 - \frac{(a-b)(b-c)(c-a)}{abc} \right],$$

$$AF \cdot BD \cdot CE = FB \cdot DC \cdot EA = DE \cdot EF \cdot FD = abc \cos \alpha \cos \beta \cos \gamma,$$

$$\frac{AF}{b} = \frac{EA}{c} = \frac{EF}{a} = \cos \alpha, \quad \frac{BD}{c} = \frac{FB}{a} = \frac{FD}{b} = \cos \beta, \quad \frac{CE}{a} = \frac{DC}{b} = \frac{DE}{c} = \cos \gamma,$$

$$\frac{AF}{FB} = \frac{\cot \alpha}{\cot \beta}, \quad \frac{BD}{DC} = \frac{\cot \beta}{\cot \gamma}, \quad \frac{CE}{EA} = \frac{\cot \gamma}{\cot \alpha},$$

$$EF = \frac{a(b^2 + c^2 - a^2)}{2bc} = a \cos \alpha, \quad FD = \frac{b(c^2 + a^2 - b^2)}{2ca} = b \cos \beta,$$

$$DE = \frac{c(a^2 + b^2 - c^2)}{2ab} = c \cos \gamma,$$

$$DE + EF + FD = \frac{8\Delta^2}{abc} = \frac{abc}{2R^2} = \frac{2rs}{R} = \frac{2\Delta}{R},$$

$$[EFA] = \Delta \cos^2 \alpha, \quad [FDB] = \Delta \cos^2 \beta, \quad [DEC] = \Delta \cos^2 \gamma,$$

$$AH = c \frac{\cos \alpha}{\sin \gamma} = 2R \cos \alpha, \quad BH = a \frac{\cos \beta}{\sin \alpha} = 2R \cos \beta, \quad CH = b \frac{\cos \gamma}{\sin \beta} = 2R \cos \gamma,$$

$$DH = b \cot \beta \cos \gamma = c \cot \gamma \cos \beta = 2R \cos \beta \cos \gamma,$$

$$EH = c \cot \gamma \cos \alpha = a \cot \alpha \cos \gamma = 2R \cos \gamma \cos \alpha,$$

$$FH = a \cot \alpha \cos \beta = b \cot \beta \cos \alpha = 2R \cos \alpha \cos \beta,$$

$$AH + BH + CH = 2(R + r),$$

$$DH + EH + FH = \frac{s^2 - 4R^2 + r^2}{2R},$$

$$[HBC] = \frac{ab}{2} \cot \beta \cos \gamma = \frac{ca}{2} \cot \gamma \cos \beta = aR \cos \beta \cos \gamma,$$

$$[HCA] = \frac{bc}{2} \cot \gamma \cos \alpha = \frac{ab}{2} \cot \alpha \cos \gamma = bR \cos \gamma \cos \alpha,$$

$$[HAB] = \frac{ca}{2} \cot \alpha \cos \beta = \frac{bc}{2} \cot \beta \cos \alpha = cR \cos \alpha \cos \beta.$$

(Wird fortgesetzt.)